$\qquad$

## Semester Quiz Review

Given the equation of the absolute value function, graph and identify the following attributes.


Transformations:
3. $\mathrm{f}(x)=-|x+3|-1$


Transformations:

Vertex:
Vertex:
Vertex:

Range:
Range:
Range:

Solve the following absolute value equations. Be sure to check for extraneous solutions, if applicable.
4. $|5-6 x|+3=10$
5. $2|2 x+6|=24$
6. $2|3 x-3|-2=14$
7. Given a table for $f(x)$. Complete a table for $h(x)$ given $h(x)=2(x-2)+4$

| $\mathbf{x}$ | $\mathbf{f}(\mathbf{x})$ |
| :---: | :---: |
| -3 | 0 |
| -1 | -3 |
| 0 | 1 |
| 1 | 0 |
| 2 | 1 |
| 3 | 0 |


8. For one day, the movie theater decided to roll back the prices to celebrate its grand opening.

Children: \$2
Adults: \$4
Senior Citizens: \$3
By the end of the day, the movie theater had sold 110 tickets and collected $\$ 344$ from ticket sales. On this day, the number of adult tickets sold was equal to the number of children tickets and senior citizen tickets combined.

Calculate the number of children, adult, and senior citizen tickets were sold. Be sure to define your variables, formulate a system of equations, and use matrices to solve the system.

For \#9-10, solve each system of two equations in two variables by hand using substitution.
9. $\left\{\begin{array}{l}y=x^{2}+x-8 \\ x+y=7\end{array}\right.$
10. $\left\{\begin{array}{l}y=x^{2}-6 x \\ -6 x+y=-32\end{array}\right.$

Solve the following systems using a calculator (matrices). Make sure to setup your matrix correctly.
11. $\left\{\begin{array}{l}-2 x+y+3 z=-8 \\ 3 x+4 y-2 z=9 \\ x+2 y+z=4\end{array}\right.$
12. $\left\{\begin{array}{l}5 y-z=16-x \\ 3 x-3 y=12-2 z \\ 2 x+z-20=-4 y\end{array}\right.$
13. $\left\{\begin{array}{l}5 y-z=-11-9 x \\ 6 x+2 z=2-4 y \\ 2 x=4-4 z+2 y\end{array}\right.$

Solve the following systems without using a calculator. (substitution and elimination).
14. $\left\{\begin{array}{l}11 x-7 y=-14 \\ x-2 y=-4\end{array}\right.$
15. $\left\{\begin{array}{l}2 x-3 y=6 \\ -4 x+6 y=6\end{array}\right.$
16. Use the quadratic formula to solve $y=2 x^{2}-12 x+8$.
17. Given a parabola with roots of $(-3,0)$ and $(7,0)$ that also passes through the point $(2,100)$, write the equation of the quadratic in standard form.
18. Describe the transformations from $f(x)=x^{2}$ to the following equations:
a) $j(x)=2 f(x-3)$
b) $k(x)=f(-x)+7$
19. You need to buy filing cabinets. You know that Cabinet $X$ costs $\$ 10$ per unit and requires six square feet of floor space. Cabinet $Y$ costs $\$ 20$ per unit and requires eight square feet of floor space. You have been given $\$ 140$ for this purchase, though you don't have to spend that much. The office has room for no more than 72 square feet of cabinets. Fill in the following information to represent this situation. (DO NOT SOLVE).

Variables:

## Objective Function:

Constraints:
20. Identify the vertex of the following quadratic by completing the square.

$$
y=2 x^{2}-4 x+8
$$

21. Describe the transformations from $p(x)$ to $m(x)$.
a. $p(x)=x^{5} ; m(x)=0.5 p(-x)+4$
b. $p(x)=x^{4} ; m(x)=-p(0.5 x)+2$

Given the equations in factored form, answer the questions.
22. $y=(1-2 x)(2 x+1)(x+4)$

Roots:

Write the multiplicity under each root.

End behavior

Sketch the graph.

Standard form: (Show Work!)
23. $y=(2 x+1)\left(4 x^{2}+4 x+1\right)$

Roots:

Write the multiplicity under each root.

End behavior

Sketch the graph.

Standard form: (Show Work!)
24. Find the remainder of the following: $\left(x^{4}+3 x^{2}+x+4\right) \div(x+3)$

Find the quotient of the following.
25. $\left(4 x^{4}-15 x^{2}-4\right) \div(x+2)$
26. $\left(x^{4}+4 x^{3}-x-4\right) \div\left(x^{3}-1\right)$

## Factor the following completely.

28. $8 x^{3}-343$
29. $\left(3 x^{3}+34 x^{2}+72 x-64\right) \div\left(x^{2}+12 x+32\right)$
30. $-4 x^{4}-500 x$
31. Write a polynomial equation given the zeros of the function are $\frac{2}{5},-3$, and 1 .
32. Write a polynomial equation given the zeros of the function are $3 \pm 2 i$ and 5 .

Solve the following inequality
32. $x^{3}+x^{2}-16 x>16$
33. $x^{3}-7 x^{2} \leq 9 x-63$

